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OPTIMIZATION OF THE LOADING FACTOR OF REGULARIZED ESTIMATED
SPATIAL-TEMPORAL WIENER FILTERS IN LARGE SYSTEM CASE.

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ABSTRACT

In this paper, it is established that the signal to interference plus
noise ratio (SINR) produced by a trained regularized Wiener spatio-
temporal filter can be estimated consistently in the asymptotic
regime where the number of receivers and the number of snapshots
converge to infinity at the same rate. The optimal regularization
parameter is estimated as the argument of the maximum of the
estimated SINR. Numerical simulations show that the proposed op-
timum regularized Wiener filter outperforms the existing regularized
spatio-temporal Wiener filters.

1. INTRODUCTION

Finite impulse response spatio-temporal Wiener filter estimation
using a training sequence is a very classical problem. When the
useful signal is corrupted by an additive temporally and spatially
white Gaussian noise, the optimal estimator is known to be the
standard least-squares estimate defined as the action of the inverse
of the empirical spatio-temporal covariance matrix on the empirical
cross correlation between the observation and the training sequence.
However, it is known for a long time that regularizing the empirical
spatio-temporal covariance matrix by a multiple of the identity
matrix may enhance the performance of the estimate because this
matrix can be ill-conditioned or even non invertible when the size
of the training sequence is smaller than the dimension of the vector
associated to the Wiener filter. The choice of the regularization
parameter appears to be a crucial issue that was addressed in a
heuristic manner in a number of references (see e.g. [10], [13, p.
748], [11] and [12]) because classical figures of merit such as the
signal to noise plus interference ratio (SINR) produced by the esti-
mated Wiener filter are difficult to estimate in the general case. In
the context of large dimension systems where the number of sensors
and the length of training sequence are both large, the situation
appears more favorable due to some subtle self-averaging effects. The
existing related works addressed the purely spatial context. Ledoit
and Wolf proposed in [9] to find the loading factor so as to minimize
the mean-square error of the estimated empirical covariance matrix,
and showed that the optimal value can be estimated consistently.
This approach was generalized in [3] to the Tyler estimator in the
the case where the array response is a priori known (no training se-
cquence) and where the noise plus interference covariance matrix is
unknown. It is shown in [7] that the SINR produced by the regular-
zated estimated Wiener filter can be consistently estimated from the
available observations, and proposed to estimate the loading factor
as the argument of the SINR maximization. The optimization of the
SINR was also considered in [14] in the context of robust estimation.

In the present paper, we assume that the observation is a M–
dimensional time series defined as a noisy output of an unknown
SIMO finite impulse response system driven by the sequence of
interest. We assume that a length N training sequence is available at
the receiver side in order to estimate a regularized degree L – 1 FIR
spatio-temporal Wiener filter from the N M–dimensional obser-
vations collected during the transmission of the training sequence.
In the large system context in which M and N both converge to-
wards +∞ at the same rate and where L remains fixed, we establish
that the SINR produced by the regularized estimated Wiener filter,
which, in principle, depends on the additive noise corrupting the
N available observations, converges towards a deterministic term
depending on the loading factor, the noise variance, assumed to be
known, and the unknown filter. We show that, while the channel fil-
ter is unknown, the above limit SINR can be estimated consistently
from the N available observations for each value of the regulariza-
tion parameter, and propose to estimate the loading factor as the
argument of its minimum.

This paper is organized as follows. In section 2 we present
the signal models and the underlying assumptions. In section 3 we
present some useful technical results proved in [6] and [8]. In sec-
tion 4 we establish that the SINR converges towards a deterministic
term, and section 5 addresses the consistent estimation of the limit
SINR. Finally, section 6 presents numerical experiments sustaining
our theoretical results, and comparing our proposal to the Ledoit-
Wolf ([9]) estimator of the regularization parameter and to other em-
pirical schemes proposed in the past ([10], [13, p. 748], [11] and
[12]).

2. PROBLEM FORMULATION.

We assume that the observation is a M–dimensional time series
(y_n)_{n \in \mathbb{Z}} defined by

\[ y_n = \sum_{p=0}^{P-1} h_p s_{n-p} + v_n, n = 1, \ldots, N \tag{1} \]

where \( h(z) = \sum_{p=0}^{P-1} h_p z^{-p} \) represents the transfer function of
the unknown FIR SIMO system and \( (v_n)_{n \in \mathbb{Z}} \) is an i.i.d sequence
of complex Gaussian random vectors with spatial covariance matrix
\( \sigma^2 \mathbf{I} \). Although \( h(z) \) is not known, we assume that P is known, i.e.
in practice, that an upper bound of the support of the impulse re-
sponse associated to \( h(z) \) is available. We assume that a length N
training sequence \( (s_n)_{n=1, \ldots, N} \) is available at the receiver side, and
estimate from \((y_n)_{n=1,...,N}\) the Wiener spatio-temporal filter \(g = (g_1, ..., g_{L-1})^T\), where the \(M\) dimensional vectors \((g_l)_{l=0,...,L-1}\) are in principle designed in such a way that \(\sum_{l=0}^{L-1} g_l y_{n+l}\) represents the minimum mean-square estimate of \(s_n\). If we denote by \(y_{n}^{(L)}\) the \(ML\)-dimensional vector defined by
\[
y_{n}^{(L)} = (y_{1,n}, ..., y_{1,n+L-1}, ..., y_{M,n}, ..., y_{M,n+L-1})^T
\]
we study the performance of the estimated regularized Wiener filter \(\hat{g}_\lambda\) defined by
\[
\hat{g}_\lambda = \left( \frac{1}{N} \sum_{n=1}^{N} y_{n}^{(L)} y_{n}^{(L)*} + \lambda I_{ML} \right)^{-1} \left( \frac{1}{N} \sum_{n=1}^{N} y_{n}^{(L)*} s_n \right)
\]
(2)

\(\hat{g}_\lambda\) is destined to estimate the unknown transmitted datas \((s_n)_{n>N}\). In the following, for each \(m = 1, ..., M\), we denote by \(H_m\) the \(L \times (P + L - 1)\) Toeplitz matrix corresponding to the convolution of signal \((s_n)_{n \in \mathbb{Z}}\) with sequence \((h_{m,p})_{p=0,...,P-1}\), and define \(ML \times (P + L - 1)\) block-Hankel matrix \(H\) by \(H = (H_1, ..., H_M)^T\). Assuming sequence \((s_n)_{n>n}\) is i.i.d., the signal to interference plus noise ratio produced by \(y_{n}^{(L)}\) is easily seen to be equal to
\[
\text{SINR}(\hat{g}_\lambda) = \frac{\|\hat{g}_\lambda h_P\|^2}{\|\hat{g}_\lambda H H^* \hat{g}_\lambda + \sigma^2 \|\hat{g}_\lambda\|^2}
\]
(3)

where \(h_P\) is column \(P\) of \(H\), and matrix \(H_1\) is obtained by deleting column \(P\) from matrix \(H\). \text{SINR}(\hat{g}_\lambda) is random in the sense that it depends on the vectors \((y_n)_{n=1,...,N}\), which are random themselves due to the presence of the additive noise. When \(N\) goes to \(+\infty\) and \(M, L\) remain fixed, it is easy to see that if \(\lambda = 0\), the filter \(g_0\) converges towards Wiener filter \((HH^* + \sigma^2 I)^{-1} h_P\) and that \(\text{SINR}(\hat{g}_0)\) converges towards \(\gamma\) defined by
\[
\gamma = \frac{h_P^* (HH^* + \sigma^2 I)^{-1} h_P}{1 - h_P^* (HH^* + \sigma^2 I)^{-1} h_P}
\]
(4)

Similar results hold when \(\lambda > 0\). On the contrary, when \(M, N\) are of the same order of magnitude, the analysis of \(\text{SINR}(\hat{g}_\lambda)\) is different and requires much more work. From now on, we assume that \(M, N \to +\infty\), the ratio \(c_N = \frac{N}{M} \to c > 0\), and \(P\) and \(L\) remain fixed.

To simplify the notations, \(N \to +\infty\) should be understood as the above asymptotic regime. In the following, it appears convenient to define by \(\Sigma\) and \(W\) the normalized \(ML \times N\) block-Hankel matrices defined by
\[
\Sigma = \frac{1}{\sqrt{N}} (y_{1}^{(L)}, ..., y_{N}^{(L)}) , \quad W = \frac{1}{\sqrt{N}} (v_{1}^{(L)}, ..., v_{N}^{(L)})
\]
respectively. Then, the relations between the available observations and sequence \((s_n)_{n=1,...,N}\) can be expressed as
\[
\Sigma = HU + W
\]
(5)

where \(U\) is the \((P + L - 1) \times N\) Hankel matrix defined by \((U_{(l)})_{l,n} = s_{n+l-P}/\sqrt{N}\). Without loss of generality, we can assume that \(UU^* = I\), it is possible to replace \(H\) by \(H(UU^*)^{1/2}\) and \(U\) by \(U(UU^*)^{-1/2}\) without modifying the model.

In the following, we define \(Q(z)\) as the resolvent of matrix \(\Sigma\Sigma^*\) defined by \(Q(z) = (\Sigma \Sigma^* - z I_{ML})^{-1}\), and remark that the estimated Wiener filter \(\hat{g}_\lambda\) can be written as
\[
\hat{g}_\lambda(z) = Q(-\lambda) \Sigma(z) u^*
\]
where \(u = \frac{1}{\sqrt{N}} (s_1, ..., s_N)\) is the \(P\)-th row of matrix \(U\). To evaluate the behaviour of the SINR given by formula (3) when \(N \to +\infty\), it is necessary to study \(|h_P^* \hat{g}_\lambda|^2, \|H_{1}^\dagger \hat{g}_\lambda\|^2\), and \(\|g_\lambda\|^2\). These terms depend on bilinear forms of matrices \(Q(-\lambda)\) and \(Q(-\lambda)^2\) whose asymptotic behaviour have thus to be evaluated. Model (5) can be interpreted as an additive spiked information plus noise model, in the sense that \(HU\) is a deterministic matrix whose rank \(P + L - 1\) does not scale with \(N\) and that \(W\) is a random matrix with zero mean elements. If \(W\) was a Gaussian random matrix with i.i.d. elements, the behaviour of the bilinear forms of \(Q(-\lambda)\) and \(Q(-\lambda)^2\) would appear as a consequence of the results of \([2]\) and \([4]\). In our context, however, the elements of matrix \(W\) are of course not i.i.d. In the present paper, we use recent results of \([6]\) and \([8]\) to establish that the bilinear forms of \(Q(-\lambda)\) and \(Q(-\lambda)^2\) behave as if \(W\) was a random matrix with i.i.d. elements.

### 3. BACKGROUND ON THE BEHAVIOUR OF MATRIX \(WW^*\).

This paper is based on a technical result which establishes that, in a certain sense, the eigenvalues of matrix \(WW^*\) behave as if the entries of \(W\) were i.i.d. In order to state the corresponding result, we recall that the Marcenko-Pastur distribution (see for example \([1]\)) with parameters \((\sigma^2, d)\) is the probability distribution defined by
\[
d\mu_d(x) = \delta_0[1-d^{-1}]+ \sqrt{(x-x^*) (x^++x)} \frac{2\sigma^2 dx}{2\sigma^2 dx} 1_{[x^-, x^+]}(x) dx
\]
with \(x^- = \sigma^2(1-\sqrt{d})^2\) and \(x^+ = \sigma^2(1+\sqrt{d})^2\). Here, \(\delta_0\) represents the Dirac measure at the origin and \(1_{[x^-, x^+]}(x) = 1\) if \(x \in [x^-, x^+]\) and 0 elsewhere. We denote by \(m_d(z)\) its Stieltjes transform defined by \(m_d(z) = \int_{\mathbb{R}} \frac{d\mu_d(\lambda)}{\lambda-z}\), and by \(\tilde{m}_d(z)\) the function \(\tilde{m}_d(z) = d m_d(z) - (1-d)/z\). These Stieltjes transform satisfy the Marcenko-Pastur canonical equations :
\[
m_d(z) = \frac{-1}{z(1 + \sigma^2 \tilde{m}_d(z))}
\]
\[
\tilde{m}_d(z) = \frac{-1}{z(1 + \sigma^2 \tilde{m}_d(z))}
\]
(6)

for each \(z \in \mathbb{C} - \mathbb{R}^+\). We denote by \(Q_W(z)\) and \(\tilde{Q}_W(z)\) the resolvent of matrices \(WW^*\) and \(WW^* - z I_{ML}\) respectively. Then, when \(N \to +\infty\), the following result holds.

**Proposition 1.** \([6, 8]\) The eigenvalue distribution of matrix \(WW^*\) converges almost surely towards the Marcenko-Pastur distribution \(\mu_d\). Moreover, if \(a_N, b_N\) are 2 unit norm \((ML)\)-dimensional deterministic vectors, then it holds that for each \(z \in \mathbb{C}^+\)
\[
a_N^* (Q_W(z) - m_{\epsilon L}(z)) b_N \to 0 \text{ a.s.}\n\]
(7)

Similarly, if \(a_N, b_N\) are 2 unit norm \(N\)-dimensional deterministic vectors, then for each \(z \in \mathbb{C}^+\), it holds that
\[
a_N^* (\tilde{Q}_W(z) - \tilde{m}_{\epsilon L}(z)) b_N \to 0 \text{ a.s.}\n\]
(8)

and that
\[
a_N^* (Q_W(z)W_N^*) b_N \to 0 \text{ a.s.}\n\]
(9)

Finally, for each \(\epsilon > 0\), convergence properties \([2, 6, 8]\) hold uniformly w.r.t. \(z\) on each compact subset of \([0, x^+ + \epsilon]\).
We recall that, roughly speaking, the convergence of the eigenvalue distribution of $W^*W^*$ towards distribution $\mu_{L,L}$ means that the histogram of the eigenvalues of any realization of $W^*W^*$ tend to accumulate around the graph of the probability density of $\mu_{L,L}$. The statements of Proposition 1 are well known when $L = 1$ and that $M$ and $N$ converge towards $+\infty$ at the same rate. The convergence towards $\mu_{L,L}$ and (7) appear as consequences of the results of [6, 8] and (7) are proved in [8].

4. ASYMPTOTIC BEHAVIOUR OF THE SINR

We recall that $Q(z) = (\Sigma \Sigma^* - zI_{M,L})^{-1}$, and define $\hat{Q}(z)$ by $\hat{Q}(z) = (\Sigma \Sigma^* - zI_N)^{-1}$. In order to simplify the notations, we omit to mention the dependency w.r.t. complex variable $z$, and put $d = El$. We introduce function $\omega(z)$ defined by $\omega(z) = \frac{1}{m_d(z)m_d(\bar{z})}$ Using (6), it is easy to obtain that $m_d(z) = \frac{1}{\omega(z)+\sigma^2}$ and $\hat{m}_d(z) = \frac{1}{\omega(z)+\sigma^2}$. If the noise matrix $W$ was i.i.d., existing results (see [2, 13]) would imply that $Q(z)$ could be approximated by

$$-\omega(z)m_d(z)(HH^* - \omega(-\lambda)I)^{-1}$$

in the sense that each bilinear form of these 2 matrices have the same asymptotic behaviour. In the same way, $Q$ could be approximated by

$$-\omega(z)m_d(z)(U^* H H U - \omega(-\lambda)I)^{-1}$$

Proposition 1 implies that (10) and (11) remain valid although $W$ is not an i.i.d. matrix. In order to establish this, we express $Q$ in terms of $\hat{Q}$ using the matrix inversion lemma, and use Proposition 1 as in [2]. Due to the lack of space, we refer the reader to a forthcoming extended version of this paper. It is possible to establish the following Proposition.

Proposition 2. When $N \to +\infty$, the three terms $||\hat{h}_p \hat{g}_s||^2$, $||H \hat{g}_s||^2$ or $||\hat{g}_s||^2$ can be approximated (i.e. have the same asymptotic behaviour) by the following deterministic quantities:

- $||\hat{h}_p \hat{g}_s||^2 \approx (h_p^* H H^* - \omega(-\lambda)I)^{-1}h_p^* (12)$

- $||H \hat{g}_s||^2 \approx \omega(-\lambda)h_p^* (H H^* - \omega(-\lambda)I)^{-2}h_p + h_p^* (H H^* - \omega(-\lambda)I)^{-1}h_p (13)$

- $||\hat{g}_s||^2 \approx \frac{\sigma^2 d}{\omega(-\lambda) - \sigma^2 d}(1 - h_p^* (H H^* - \omega(-\lambda)I)^{-1}h_p) + \frac{\sigma^2 d}{\omega(-\lambda) - \sigma^2 d} h_p^* (H H^* - \omega(-\lambda)I)^{-2}h_p$ (14)

Moreover, if we introduce $\alpha(\lambda) = h_p^* (H H^* - \omega(-\lambda)I)^{-1}h_p^*$ and $\beta(\lambda) = h_p^* (H H^* - \omega(-\lambda)I)^{-2}h_p^*$, it holds that

$$\text{SINR}(\hat{g}_s^L) - \phi(\lambda) \to 0$$

almost surely, where $\phi(\lambda)$ is defined by

$$\phi(\lambda) = \frac{\alpha(\lambda)^2}{[1 - \alpha(\lambda)][\alpha(\lambda) + \frac{\sigma^2 d}{\omega(-\lambda) - \sigma^2 d} + \frac{\omega^2(\omega(-\lambda) + \sigma^2 d)}{\omega(-\lambda) - \sigma^2 d} \beta(\lambda)]}$$

(15)

When $cL < 1$, it is possible to consider the case where $\lambda = 0$. Using the observation that $\omega(0) = -\sigma^2$, we obtain immediately that $\phi(0) = \frac{1 - cL}{\gamma + cL}$

$$\phi(0) = \gamma \frac{(1 - cL) \gamma}{\gamma + cL}$$

(17)

where $\gamma$ is the SINR corresponding to the true Wiener filter (see formula 1). Consequently, the estimation of the Wiener filter by $\hat{g}_s^{(0)}$ produces a SINR loss equal to $(1 - cL) \frac{\gamma}{\gamma + cL}$, which of course, is considerable when $cL$ is close from 1. As shown below, the use of a convenient regularization coefficient allows to improve considerably the SINR.

5. CONSISTENT ESTIMATORS OF THE SINR

It is clear that function $\lambda \to \phi(\lambda)$ depends on matrix $H$ which is unknown. We establish in this section that it is possible to estimate $\phi(\lambda)$ consistently for each $\lambda > 0$. For this, it is sufficient to estimate $\alpha(\lambda)$ and $\beta(\lambda)$ (see (16)). It is easy to see that

$$\alpha(\lambda) = 1 + \omega(-\lambda)((H^* H - \omega(-\lambda)I)^{-1})p_r$$

By (10) and (11), $(H^* H - \omega(-\lambda)I)^{-1}p_r$ can be estimated by

$$\hat{\alpha}(\lambda) = 1 - \frac{u \hat{Q}(-\lambda)u^*}{\hat{m}_d(-\lambda)}$$

(18)

is a consistent estimate of $\alpha(\lambda)$. In order to obtain an estimator $\hat{\beta}(\lambda)$ of $\beta(\lambda)$, we observe that

$$h_p^* (H H^* - \omega(-\lambda)I)^{-2}h_p = \omega(-\lambda)((H^* H - \omega(-\lambda)I)^{-1})p_r$$

By (11), $U \hat{Q}(-\lambda)u = \hat{m}_d(z)\omega(z)((H^* H - \omega(-\lambda)I)^{-1})p_r$. Multiplying by $z$ and taking the derivative w.r.t. $z$ leads to the conclusion that it is possible to estimate consistently $(H H^* - \omega(-\lambda)I)^{-2}$ by:

$$\frac{\omega^2(-\lambda) - \sigma^2 d}{\omega(-\lambda) + \sigma^2 d} z \hat{Q}(z) \frac{d}{dz} z \hat{Q}(z) u^*$$

From this, we obtain that $\beta(\lambda)$ can be estimated consistently by the term $\hat{\beta}(\lambda)$ defined by

$$\hat{\beta}(\lambda) = -\frac{\sigma^2 d}{\omega(-\lambda) + \sigma^2 d} \left[ u \hat{Q}(-\lambda) - \lambda \hat{Q}(-\lambda)u^* \right]$$

(19)

Replacing $\alpha(\lambda)$ and $\beta(\lambda)$ by $\hat{\alpha}(\lambda)$ and $\hat{\beta}(\lambda)$ in formula (16), we obtain immediately a consistent estimator $\hat{\phi}(\lambda)$ of the asymptotic SINR $\phi(\lambda)$. Moreover, it is possible to establish that function $\phi(\lambda) - \hat{\phi}(\lambda)$ converges uniformly towards 0 on each compact subset of $\mathbb{R}^+$. Therefore, if we denote by $\lambda_{opt}$ and $\hat{\lambda}_{opt}$ the argument of the maximum of $\phi$ and $\hat{\phi}$ on a fixed compact of $\mathbb{R}^+$, it holds that $\lambda_{opt} - \hat{\lambda}_{opt} \to 0$. Therefore, maximizing function $\lambda \to \phi(\lambda)$ allows to estimate a regularization parameter for which the true asymptotic SINR $\phi(\lambda)$ is maximum. We also notice that this approach allows to choose the smoothing factor $L$: it is sufficient to evaluate $\phi(\hat{\lambda}_{opt})$ for each choice of $L$, and to select the smoothing factor for which the latter term is maximum. This is of course not a computationally efficient procedure because it needs to evaluate matrix $Q(-\lambda)$ at $\hat{\lambda}_{opt}(-\lambda)$ for each $\lambda$ and each integer $L$. 

6. NUMERICAL EXPERIMENTS.

In this section, we provide numerical simulations illustrating the results given in the previous sections. We first illustrate the accuracy of the approximation $\text{SINR}(\hat{g}_L) \approx \phi(\lambda)$ where we recall that $\text{SINR}(\hat{g}_L)$ is the true SINR defined by $\lambda$. Matrix $(H_0, \ldots, H_{P-1})$ is a realization of a normalized version (so as to obtain a Frobenius norm equal to 1) of random matrix $(a(\theta_0), \ldots, a(\theta_{P-1}))$, with $a(\theta) = \frac{1}{\sqrt{N}}(1, \ldots, e^{i(M-1)\theta})^T$, and where the angles are drawn uniformly on $[0, 2\pi]$. The sequence $(s_n)_{n=1, \ldots, N}$ is a realization of an i.i.d ±1 sequence with probability 1/2. The signal to noise ratio SNR is thus equal to 1/$\sigma^2$. In the following experiments, $N = 200$, $M = 40$ and $P = 5$. In figure 1 SNR is equal to 8dB, $L = 5$, and we evaluate by Monte-Carlo simulations (10,000 realizations are generated) function $\lambda \rightarrow \text{SINR}(\hat{g}_L^{(L)})$. We represent the graph of the function $\phi(\lambda)$ along with 2 plots representing the lower and upper bounds of the 95% confidence interval of $\lambda \rightarrow \text{SINR}(\hat{g}_L^{(L)})$. We can notice that the 3 graphs are close one from each other.

We finally justify that our approach may be used in order to estimate a relevant value of the smoothing parameter $L$. As mentioned above, we evaluate $\phi(\lambda_{opt})$ for each possible value of $L$, and propose to select the value of $L$ for which the latter term is maximum. We keep the same parameters as above. We first represent in figure 2 function $\lambda \rightarrow \phi(\lambda)$ for $L = 1, 2, 3, 4, 5, 6, 7, 8$, and conclude that $L = P = 5$ maximizes $\phi(\lambda_{opt})$, but that $L = 6, 7, 8$ also provide reasonable optimum asymptotic SINR. We can also check that choosing in a convenient way $L$ and $\lambda$ may improve considerably the SINR.

7. CONCLUSION

In this paper, we have proposed a new approach to evaluate the loading factor of a regularized estimated spatio-temporal Wiener filter in the context of large systems. Assuming that the number of sensors $M$ and the length of the training sequence $N$ are large and of the same order of magnitude, and that the degrees of the Wiener filter and of filter $H(z)$ do not scale with $M, N$, we have established that the SINR provided by the estimated regularized Wiener filter converges towards an expression depending on the noise variance, the channel coefficients, and the loading factor. This limit SINR can be consistently estimated, and we have proposed to estimate the regularization factor as the argument of the maximum of the estimated limit SINR. Simulation results have shown that the proposed approach allows to considerably improve the results provided by existing approaches.
8. REFERENCES


